Homework 8

1. An amateur gardener wanted to discover whether one fertilizer is better than another when applied to his tomato plants. Having taken a statistics course in the design of experiments, this gardener knew that conditions for all 11 of his tomato plants must be the same so that the effects of applying the two different fertilizers will not be confounded by something else. Therefore, he planted the 11 tomato plants of the same hybrid in the same plot with the same exposure to sunlight, etc. He applied fertilizer A to five tomato plants which were chosen at random, and he applied fertilizer B to six other tomato plants. At harvest, the average weight of a tomato from each plant was obtained and is tabulated below:

Average Weight of a Tomato					
Fertilizer A	Fertilizer B				
29.9 oz	26.6 oz				
11.4	23.7				
25.3	28.5				
16.5	14.2				
21.1	17.9				
	24.3				

Is there a difference in the yield due to the different fertilizers at the .05 level of significance? (Hint:Test the hypothesis: $H_0: \mu_1 - \mu_2 = 0$ vs $H_1: \mu_1 - \mu_2 \neq 0$).

- 2. A farmer claims that the average yield of corn of variety A exceeds the average yield of variety B by at least 12 bushels per acre. To test this claim, 20 one acre plots of each variety are planted and grown under similar conditions. Variety A yielded, on the average, 86.7 bushels per acre with a sample standard deviation of 6.28 bushels per acre, while variety B yielded, on the average, 77.8 bushels per acre with a sample standard deviation of 5.61 bushels per acre. Test the farmer's claim using a .05 level of significance. (Hint: Test the hypothesis: $H_0: \mu_1 \mu_2 = 12$ vs $H_1: \mu_1 \mu_2 > 12$).
- 3. Let $\bar{x}_1 = 61, 600, n_1 = 12$, and $s_1 = 3300$. Let $\bar{x}_2 = 64, 000, n_2 = 12$, and $s_2 = 3500$. Assume that $\sigma_1^2 = \sigma_2^2$. Test the hypothesis:

$$H_0: \mu_1 - \mu_2 = 0$$
 vs $H_1: \mu_1 - \mu_2 \neq 0$ at $\alpha = .05$

4. A Cuckoo will lay eggs in the nests of other birds. It is claimed by some biologists that the size of an egg which a Cuckoo will lay conforms to the size of the egg of a warbler or of a wren depending in which nest the Cuckoo lays her egg. The following descriptive statistics given in Table 1 were obtained for Cuckoo eggs which were found in randomly sampled nests of warblers and wrens. Test the hypothesis: H₀ : μ₁ − μ₂ = 0 vs H₁ : μ₁ − μ₂ ≠ 0 at a level of significance of .01 where #1 designates the population of warbler nests and #2 designates the population of wren nests.

Table 1:

	#1	#2
n	29	35
\bar{x}	22.20 mm	21.12 mm
S	.65 mm	.75 mm

5. Residents usually welcome the installation of speed humps on their streets in order to reduce speeding traffic whereas traffic engineers despise speed humps because by impeding cut-through traffic they divert cut-through traffic onto the arterial routes. The engineers recorded the speeds before and after the installation of speed humps to see if they have an effect. A tabulation of speeds on some selected streets are given below. At a level of $\alpha = .10$, can the engineers conclude that speed humps on the average reduce the speed of traffic by 10 mph?

Street	Before	After	
Northborne Drive	45 mph	33 mph	
Kings Park Drive	50	27	
Hollinger Avenue	43	28	
Springhaven Drive	40	30	

6. A company bakes computer chips in two ovens, A and B. Chips are randomly assigned to an oven and hundreds of chips are baked each hour. The percentage of defective chips are tabulated below. For example, oven A produced chips which were 45% defective during hour 1. Does there appear a difference between oven A and oven B with respect to the rate of producing defective chips at a 95% level of significance?

	1 45% 36%	2	3	4	5	6	7	8	9
Α	45%	32	34	31	35	37	31	30	27
В	36%	37	33	34	33	32	33	30	24