STAT112: Mock-Midterm Examination

- 1. On an examination in psychology, 12 students in one class had a sample mean grade of 78 with a sample standard deviation of 6, while 15 students in another class had a sample mean grade of 74 with a sample standard deviation of 8. Using a level of significance of .05, determine whether the first group is superior to the second group.
- 2. What is the difference between these two estimators: $\widehat{E[y_i]}$ and $\hat{y_i}$ where y_i is the response variable of a linear model?
- 3. Given the samples, $S_1 = \{6\ 2\ 1\ 3\ 3\}$ and $S_2 = \{5\ 3\ 2\ 4\ 2\}$, test the hypothesis: $H_0: \mu_1 = \mu_2$ vs $H_1: \mu_1 \neq \mu_2$ at the .05 level of significance.
- 4. Using the same two samples of problem 3, find the 95% CI of $\mu_2 \mu_1$.
- 5. Let t_0 represent a particular value of Student's t distribution. Find the value of t_0 which will make the following statement true: $P(t \le -t_0)$ or $t \ge t_0 = .10$ with df=12.
- 6. A random sample of 36 drinks from a soft-drink machine has an average content of 8 ounces with a standard deviation of .48 ounces. The vendor claims that the machine gives 7.5 ounces per cup. Are the customers being given too much? That is, test the hypothesis: $H_0: \mu = 7.5$ ounces vs $H_1: \mu > 7.5$ ounces at the .05 level of significance.
- 7. Given the following data of the rate by which laborers per 100 quit their jobs and of their hourly wage, a linear fixed effects model was proposed where the response variable is the rate of attrition and the explanatory variable is the average wage.

| Rate of Attrition | 1.4 | .7 | 2.6 | 3.4 | 1.7 | 1.7 | 1.0 | .5 |
|-------------------|-------|-------|------|-------|------|------|-------|-------|
| Average Wage | \$8.2 | 10.35 | 6.18 | 5.37 | 9.94 | 9.11 | 10.59 | 13.29 |
| Age | 36 | 45 | 25 | 20 | 44 | 40 | 46 | 55 |
| Rate of Attrition | 2.3 | 1.9 | 1.4 | 1.8 | 2.0 | 2.0 | 3.8 | |
| Average Wage | \$7.5 | 6.43 | 8.83 | 10.93 | 8.80 | 7.99 | 5.549 | |
| Age | 35 | 21 | 33 | 27 | 39 | 47 | 39 | |

- (a) Write the two parameter fixed effects linear model where the response variable is rate of attrition and the explanatory variable is average wage:
- (b) Compute $\hat{\beta}_0$ =
- (c) Compute $\hat{\beta}_1$ =
- (d) When the wage is \$7.50 per hour, what is the estimate of the expected rate of attrition?
- (e) Find the 95% confidence interval for that predicted sample average, $E[\widehat{E[y_i]}]$.

Table 1: Analysis of Variance for Fitting Regression

| Source of Variation | df | Sum of Squares | Mean Sum of Squares | F statistic |
|---------------------|----|----------------|---------------------|-------------|
| Mean | | | | |
| Regression | | | | |
| Residual Error | | | | |
| Total | | | | |

- (f) Test the hypothesis, $H_0: \beta_1 = 0$ vs $H_1: \beta_1 \neq 0$ at a level of significance, $\alpha = .05$. $F_{r-1,n-r,\alpha}$ =
- (g) Give s=
- (h) Compute the 95% confidence interval for β_1 .
- (i) An age*wage interaction term is added to the model. Write this model:
- (j) The resulting abbreviated ANOVA is given in Table 2

Table 2: Analysis of Variance for Fitting Regression

| Source of Variation | df | Sum of Squares | Mean Sum of Squares | p-value |
|---------------------|----|----------------|---------------------|----------|
| wage | 1 | 8.2507 | 39.8792 | 3.86e-05 |
| age*wage | 1 | 0.5906 | 2.8547 | 0.1169 |
| Residual Error | 12 | 2.4827 | | |

- i. Is the interaction term significant at a level of significance of .05? Explain.
- ii. The estimate of the interaction coefficient is: 0.016743. (The estimate of β_0 is: 10.317015 and the estimated wage coefficient is: -1.640321.) Interpret what this estimate of the interaction coefficient means to someone who never took statistics.
- 8. One die is tossed 180 times with the following results:

Is the die fair? Use a .01 level of significance.

9. An association of homeowners of a residential sub-division requested from the local jurisdiction painted crosswalks to be placed across a busy street where there are a school bus and municipal bus stops arguing that the crosswalks will improve the safety of their children and pedestrians. The state traffic engineer argued against the proposal saying that out of 54,750,000 vehicles passing by that spot in the past ten years, only two accidents occurred and none with pedestrians. Therefore, based on accident statistics spending \$200 for painted crosswalks is not justified. Is the statistical argument convincing? Explain.